

# NAG C Library Function Document

## nag\_zhptri (f07pwc)

### 1 Purpose

nag\_zhptri (f07pwc) computes the inverse of a complex Hermitian indefinite matrix  $A$ , where  $A$  has been factorized by nag\_zhptrf (f07prc), using packed storage.

### 2 Specification

```
void nag_zhptri (Nag_OrderType order, Nag_UptoType uplo, Integer n, Complex ap[],  
     const Integer ipiv[], NagError *fail)
```

### 3 Description

To compute the inverse of a complex Hermitian indefinite matrix  $A$ , this function must be preceded by a call to nag\_zhptrf (f07prc), which computes the Bunch–Kaufman factorization of  $A$  using packed storage.

If **uplo** = **Nag\_Upper**,  $A = PUDU^H P^T$  and  $A^{-1}$  is computed by solving  $U^H P^T XPU = D^{-1}$  for  $X$ .

If **uplo** = **Nag\_Lower**,  $A = PLDL^H P^T$  and  $A^{-1}$  is computed by solving  $L^H P^T XPL = D^{-1}$  for  $X$ .

### 4 References

Du Croz J J and Higham N J (1992) Stability of methods for matrix inversion *IMA J. Numer. Anal.* **12** 1–19

### 5 Parameters

1: **order** – Nag\_OrderType *Input*

*On entry:* the **order** parameter specifies the two-dimensional storage scheme being used, i.e., row-major ordering or column-major ordering. C language defined storage is specified by **order** = **Nag\_RowMajor**. See Section 2.2.1.4 of the Essential Introduction for a more detailed explanation of the use of this parameter.

*Constraint:* **order** = **Nag\_RowMajor** or **Nag\_ColMajor**.

2: **uplo** – Nag\_UptoType *Input*

*On entry:* indicates how  $A$  has been factorized as follows:

if **uplo** = **Nag\_Upper**,  $A = PUDU^H P^T$ , where  $U$  is upper triangular;

if **uplo** = **Nag\_Lower**,  $A = PLDL^H P^T$ , where  $L$  is lower triangular.

*Constraint:* **uplo** = **Nag\_Upper** or **Nag\_Lower**.

3: **n** – Integer *Input*

*On entry:*  $n$ , the order of the matrix  $A$ .

*Constraint:*  $n \geq 0$ .

4: **ap**[*dim*] – Complex *Input/Output*

**Note:** the dimension, *dim*, of the array **ap** must be at least  $\max(1, n \times (n + 1)/2)$ .

*On entry:* details of the factorization of  $A$  stored in packed form, as returned by nag\_zhptrf (f07prc).

*On exit:* the factorization is overwritten by the  $n$  by  $n$  Hermitian matrix  $A^{-1}$  stored in packed form.

5:	<b>ipiv</b> [dim] – const Integer	<i>Input</i>
<b>Note:</b> the dimension, dim, of the array <b>ipiv</b> must be at least $\max(1, \mathbf{n})$ .		
6:	<b>fail</b> – NagError *	<i>Output</i>
The NAG error parameter (see the Essential Introduction).		

## 6 Error Indicators and Warnings

### NE\_INT

On entry, **n** =  $\langle \text{value} \rangle$ .

Constraint: **n**  $\geq 0$ .

### NE\_SINGULAR

The block diagonal matrix  $D$  is exactly singular.

### NE\_ALLOC\_FAIL

Memory allocation failed.

### NE\_BAD\_PARAM

On entry, parameter  $\langle \text{value} \rangle$  had an illegal value.

### NE\_INTERNAL\_ERROR

An internal error has occurred in this function. Check the function call and any array sizes. If the call is correct then please consult NAG for assistance.

## 7 Accuracy

The computed inverse  $X$  satisfies a bound of the form

if **uplo** = **Nag\_Upper**,  $|DU^T P^T XPU - I| \leq c(n)\epsilon(|D| |U^T| |P^T| |X| |P| |U| + |D| |D^{-1}|)$ ;

if **uplo** = **Nag\_Lower**,  $|DL^T P^T XPL - I| \leq c(n)\epsilon(|D| |L^T| |P^T| |X| |P| |L| + |D| |D^{-1}|)$ ,

$c(n)$  is a modest linear function of  $n$ , and  $\epsilon$  is the **machine precision**.

## 8 Further Comments

The total number of real floating-point operations is approximately  $\frac{8}{3}n^3$ .

The real analogue of this function is **nag\_dsptri** (f07pjc).

## 9 Example

To compute the inverse of the matrix  $A$ , where

$$A = \begin{pmatrix} -1.36 + 0.00i & 1.58 + 0.90i & 2.21 - 0.21i & 3.91 + 1.50i \\ 1.58 - 0.90i & -8.87 + 0.00i & -1.84 - 0.03i & -1.78 + 1.18i \\ 2.21 + 0.21i & -1.84 + 0.03i & -4.63 + 0.00i & 0.11 + 0.11i \\ 3.91 - 1.50i & -1.78 - 1.18i & 0.11 - 0.11i & -1.84 + 0.00i \end{pmatrix}.$$

Here  $A$  is Hermitian indefinite, stored in packed form, and must first be factorized by **nag\_zhpstrf** (f07prc).

## 9.1 Program Text

```

/* nag_zhptri (f07pwc) Example Program.
*
* Copyright 2001 Numerical Algorithms Group.
*
* Mark 7, 2001.
*/
#include <stdio.h>
#include <nag.h>
#include <nag_stdlb.h>
#include <nagf07.h>
#include <nagx04.h>

int main(void)
{
    /* Scalars */
    Integer ap_len, i, j, n;
    Integer exit_status=0;
    NagError fail;
    Nag_UptoType uplo_enum;
    Nag_OrderType order;

    /* Arrays */
    Integer *ipiv=0;
    char uplo[2];
    Complex *ap=0;

#ifdef NAG_COLUMN_MAJOR
#define A_UPPER(I,J) ap[J*(J-1)/2 + I - 1]
#define A_LOWER(I,J) ap[(2*n-J)*(J-1)/2 + I - 1]
    order = Nag_ColMajor;
#else
#define A_LOWER(I,J) ap[I*(I-1)/2 + J - 1]
#define A_UPPER(I,J) ap[(2*n-I)*(I-1)/2 + J - 1]
    order = Nag_RowMajor;
#endif

    INIT_FAIL(fail);
    Vprintf("f07pwc Example Program Results\n\n");

    /* Skip heading in data file */
    Vscanf("%*[^\n] ");
    Vscanf("%ld%*[^\n] ", &n);
    ap_len = n * (n + 1)/2;

    /* Allocate memory */
    if ( !(ipiv = NAG_ALLOC(n, Integer)) ||
        !(ap = NAG_ALLOC(ap_len, Complex)) )
    {
        Vprintf("Allocation failure\n");
        exit_status = -1;
        goto END;
    }
    /* Read A from data file */
    Vscanf(" ', %ls '%*[^\n] ", uplo);
    if (*(unsigned char *)uplo == 'L')
        uplo_enum = Nag_Lower;
    else if (*(unsigned char *)uplo == 'U')
        uplo_enum = Nag_Upper;
    else
    {
        Vprintf("Unrecognised character for Nag_UptoType type\n");
        exit_status = -1;
        goto END;
    }
    if (uplo_enum == Nag_Upper)
    {
        for (i = 1; i <= n; ++i)
        {

```

```

        for (j = i; j <= n; ++j)
            Vscanf(" ( %lf , %lf )", &A_UPPER(i,j).re, &A_UPPER(i,j).im);
    }
    Vscanf("%*[^\n] ");
}
else
{
    for (i = 1; i <= n; ++i)
    {
        for (j = 1; j <= i; ++j)
            Vscanf(" ( %lf , %lf )", &A_LOWER(i,j).re, &A_LOWER(i,j).im);
    }
    Vscanf("%*[^\n] ");
}

/* Factorize A */
f07prc(order, uplo_enum, n, ap, ipiv, &fail);
if (fail.code != NE_NOERROR)
{
    Vprintf("Error from f07prc.\n%s\n", fail.message);
    exit_status = 1;
    goto END;
}
/* Compute inverse of A */
f07pwc(order, uplo_enum, n, ap, ipiv, &fail);
if (fail.code != NE_NOERROR)
{
    Vprintf("Error from f07pwc.\n%s\n", fail.message);
    exit_status = 1;
    goto END;
}
/* Print inverse */
x04ddc(order, uplo_enum, Nag_NonUnitDiag, n, ap,
        Nag_BracketForm, "%7.4f", "Inverse", Nag_IntegerLabels,
        0, Nag_IntegerLabels, 0, 80, 0, 0, &fail);
if (fail.code != NE_NOERROR)
{
    Vprintf("Error from x04ddc.\n%s\n", fail.message);
    exit_status = 1;
    goto END;
}
END:
if (ipiv) NAG_FREE(ipiv);
if (ap) NAG_FREE(ap);

return exit_status;
}

```

## 9.2 Program Data

```
f07pwc Example Program Data
4                                     :Value of N
'L'                                    :Value of UPLO
(-1.36, 0.00)
( 1.58,-0.90) (-8.87, 0.00)
( 2.21, 0.21) (-1.84, 0.03) (-4.63, 0.00)
( 3.91,-1.50) (-1.78,-1.18) ( 0.11,-0.11) (-1.84, 0.00) :End of matrix A
```

## 9.3 Program Results

f07pwc Example Program Results

Inverse	1	2	3	4
1 ( 0.0826, 0.0000)	(	)	(	
2 (-0.0335, 0.0440)	(	)	(	
3 ( 0.0603,-0.0105)	(	)	(	
4 ( 0.2391,-0.0926)	(	)	(	